Routing for Relief Efforts

Minimising Response Time in Natural Disasters



Outline

- Motivation
- Research Question
- Method
- Experiments
- Conclusion



Motivation

- Rescue of people during natural disasters
- Minimizing Response Time
- Vehicle Routing Problem



Turkey Earthquake 2023 Destruction [im1]



Depot
 Recipient

Last-Mile Delivery Problem Instance Example [1] Marvin Beese - Routing for Relief Efforts







Minimizing Response Time of Relief Vehicles



Method – MinMax, MinSum

- Network of Recipients
- Directed tours
- Objective functions for optimization
 - Minimization of the Maximum arrival time (MinMax)
 - Minimization of the Summation of arrival times (MinSum)







(b) minmax is different from minsum [2]

Method – Theoretical Considerations

- Graph-network G = (R, E, W)
 - Recipients $R = \{r_1, \dots, r_m\}$
 - Edges $E = \{(e_{lk}) | e_{lk} \text{ connects } r_l, r_k \in R, l \neq k\}$
 - Weights $W = \{w_{lk} | w_{lk} \text{ corresponds to } e_{jk}\}$
- Capacity:
 - \forall Vehicles n_i , \exists capacity c_i





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- Capacity:
 - \forall Vehicles n_i , \exists capacity c_i
- + Feasibility:
 - Vehicle n_i can reach recipient r_j
- + Demand:
 - \forall Recipients r_j , \exists demand d_j
- + Deadline:
 - \forall Recipients r_j , \exists deadline t_j











Method – Programmatical Implementation



Method – Programmatical Implementation



Method – Programmatical Implementation



TSP, MinMax and MinSum with Notes [2]

| • Integra | tion of |
|-----------|---------|
|-----------|---------|

- Capacities
- Feasibilities
- Demands
- Deadlines

| -API |
|------|
|------|

|-Carthography |-Routing |-Seismic

|-Routing

|-Directional |-Permutational |-Distantial

|-Solver

|-MinSum

|-MinMax

|-Instanciation

|-Depot

|-Vehicle

|-Capacities

Experiments

- Theoretical Setting:
 - Graph with 1 depot and 4 recipients
 - Different distances
 - Uniform capacities



| individual vehicle costs | Approach | | | | | | | | | |
|--------------------------|----------------|----------------|----------------|------------------------|--|--|--|--|--|--|
| | Basic | Feasibility | Deadline | Feasibility + Deadline | | | | | | |
| MinMax | v1: 27, v2: 22 | v1: 20, v2: 37 | v1: 15, v2: 34 | v1: 20, v2: 24 | | | | | | |
| MinSum | v1: 27, v2: 22 | v1: 20, v2: 24 | v1: 29, v2: 27 | v1: 29, v2: 27 | | | | | | |

Table 1. Individual vehicle costs for inexact implementations of the MinSum and MinMax

Experiments

- Real-World Setting
 - Graph with 4 recipients
 - Real-world coordinates
 - Capacitated MinSum insertion algorithm
 - 2 vehicles



Conclusion

- Relief Routing with MinMax and MinSum Algorithms
- Integration of additional heuristics: Feasibilities, Demand, Deadlines
- Embedding of Cartography and Seismic activity with real-world and live data
 - End-to-End Integration: Instantiation \rightarrow Visualization
- Future Work: Dealing with Uncertainties, Extensive Experiments





References

[1] M. Huang, K. Smilowitz, and B. Balcik, "Models for relief routing: equity, efficiency and efficacy," Procedia-social and behavioral sciences, vol. 17, pp. 416–437, 2011.

[2] A. M. Campbell, D. Vandenbussche, and W. Hermann, "Routing for relief efforts," Transportation science, vol. 42, no. 2, pp. 127–145, 2008.

[im1] Satellite image ©2023 Maxar Technologies Handout. (Reuters),

https://english.alarabiya.net/News/world/2023/02/09/Satellite-images-show-Turkey-before-andafter-tragic-quake-that-killed-over-16-000

[im2] Earth Systems Science Data – MDAS: a new multimodal benchmark dataset for remote sensing <u>https://essd.copernicus.org/articles/15/113/2023/</u>



scienceof

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https://github.com/bmarv/relief-routing-models

Intelligence https://www.scienceofintelligence.de/people/marvin-beese/



Backup – Feasibilities & Deadlines

| Algorithm 1 Pseudocode of the Minmax-Insertion Algorithm with Feasibilities and Deadlines |
|--|
| 1: function MINMAXINSERTION(distances, demands, capacites, deadlines, feasibilities) |
| 2: $num_nodes, num_routes, routes, loads \leftarrow$ initiation from overloaded arguments |
| 3: $sorted_nodes \leftarrow$ sorting in ascending order based on their deadlines |
| 4: for node in sorted_nodes do |
| 5: $best_cost \leftarrow +\infty$ |
| 6: $best_vehicle \leftarrow -1$ |
| 7: $best_position \leftarrow -1$ |
| 8: $node_usability \leftarrow check wrt. feasibility, demand(node) and vehicle(loads)$ |
| 9: for vehicle in range(num_routes) do |
| 10: if vehicle \leftarrow feasible and deadline \leftarrow fulfillable and vehicle_capacity \leftarrow sufficient then |
| 11: $current_cost \leftarrow calculate_route_cost$ |
| 12: $insertion_cost \leftarrow cost_of_inserting(node, position, \forall vehicles_on_route)$ |
| 13: if $insertion_cost < best_cost$ then |
| 14: $best_cost \leftarrow insertion_cost$ |
| 15: $best_vehicle \leftarrow vehicle$ |
| 16: $best_position \leftarrow position$ |
| 17: end if |
| 18: end if |
| 19: end for |
| 20: insert node into routes[best_vehicle] at position best_position |
| 21: $loads[best_vehicle] \leftarrow loads[best_vehicle] + demands[node]$ |
| 22: end for |
| 23: return <i>routes</i> |
| 24: end function |

Backup – Cost Algorithms

Algorithm 2 Cost Algorithms in Pseudocode

```
function CALCULATECOST(distance_matrix, route)

\cot \leftarrow 0

for i from 0 to length(route) - 2 do

from_node \leftarrow route[i]

to_node \leftarrow route[i + 1]

\cot \leftarrow \cot + \operatorname{distance\_matrix[from\_node][to\_node]}

end for

return cost

end function
```

```
function CALCULATEINSERTIONCOST(dist_mat, route, position, node)
from_node assignment
to_node assignment
insertion_cost ← dist_mat[from_node][node] + dist_mat[node][to_node] - dist_mat[from_node][to_node]
return insertion_cost
end function
```

Backup – TSP vs. MinMax or MinSum

- *la* := latest arrival time
- *sa* := sum of arrivals
- us := mean absolute upper semideviation [11]
 - $\frac{1}{n}\sum_{a_i\geq\mu}(a_i-\mu)$
 - smaller us: equity ↑
- c := total route duration

- results with shorter *la* & better
 us, but higher *c* for minmax
 compared to TSP
- results with shorter *la* & better
 us, but higher *c* for minsum
 compared to TSP

$$la(\frac{TSP}{MinMax}) > 1$$



| | | $\frac{la(TSP)}{la(MM)}$ | $\frac{la(MS)}{la(MM)}$ | $\frac{sa(TSP)}{sa(MS)}$ | $\frac{sa(MM)}{sa(MS)}$ | $\frac{c(MM)}{c(TSP)}$ | $\frac{c(MS)}{c(TSP)}$ | $\frac{us(TSP)}{us(MM)}$ | $\frac{us(TSP)}{us(MS)}$ | $rac{us(MM)}{us(MS)}$ |
|-----------|-----|--------------------------|-------------------------|--------------------------|-------------------------|------------------------|------------------------|--------------------------|--------------------------|------------------------|
| Augerat-A | MIN | 0.948 | 0.970 | 0.974 | 0.973 | 1.004 | 1.027 | 0.926 | 0.902 | 0.850 |
| | MAX | 1.051 | 1.257 | 1.229 | 1.270 | 1.246 | 1.431 | 1.114 | 1.138 | 1.234 |
| | AVG | 1.013 | 1.114 | 1.089 | 1.124 | 1.075 | 1.184 | 1.016 | 1.016 | 1.003 |
| Augerat-B | MIN | 0.912 | 0.922 | 0.852 | 0.938 | 0.995 | 0.963 | 0.822 | 0.730 | 0.728 |
| | MAX | 1.146 | 1.275 | 1.424 | 1.321 | 1.233 | 1.384 | 1.391 | 1.565 | 1.315 |
| | AVG | 1.020 | 1.092 | 1.061 | 1.074 | 1.047 | 1.114 | 1.041 | 1.068 | 0.987 |
| Golden | MIN | 0.977 | 0.966 | 1.006 | 1.020 | 1.012 | 1.007 | 0.951 | 0.955 | 0.901 |
| | MAX | 1.049 | 1.263 | 1.185 | 1.210 | 1.095 | 1.303 | 1.089 | 1.080 | 1.052 |
| | AVG | 1.014 | 1.115 | 1.105 | 1.101 | 1.055 | 1.167 | 1.003 | 1.017 | 0.987 |





[2]

Backup – VRP vs TSP

- consideration of additional vehicles
- ratio gets significantly larger with multiple vehicles
 - $\frac{Ia(VRP)_Q^k}{Ia(MM)_Q^k}$
 - $\frac{sa(VRP)_Q^k}{sa(MS)_Q^k}$
- cost increases are not as significant

| | | | $la(VRP)_{0}^{k}$ | ° C | $c(MM)_{O}^{k}$ | | | $ us(VRP)_O^k$ | | | | | |
|-----------|-----|------------------------|-------------------|--------|----------------------------|-------|-------|------------------------|--|-------|-------|--------|-----|
| | | $\frac{1}{la(MM)_Q^k}$ | | | $\frac{1}{c(VRP)_{O}^{k}}$ | | | $\frac{1}{us(MM)_Q^k}$ | | | | | |
| | | k = 1 | k = 5 | k = 10 | | k = 1 | k = 5 | k = 10 | | k = 1 | k = 5 | k = 10 | |
| Augerat-A | MIN | 0.948 | 1.050 | 1.170 | | 1.004 | 1.044 | 1.067 | | 0.926 | 0.942 | 0.993 | |
| | MAX | 1.051 | 1.618 | 1.627 | | 1.246 | 1.220 | 1.370 | | 1.114 | 1.376 | 1.305 | |
| | AVG | 1.013 | 1.365 | 1.390 | | 1.075 | 1.122 | 1.212 | | 1.016 | 1.163 | 1.150 | |
| Augerat-B | MIN | 0.912 | 0.890 | 1.066 | | 0.995 | 1.013 | 0.994 | | 0.822 | 0.622 | 0.771 | _ |
| | MAX | 1.146 | 2.129 | 2.047 | | 1.233 | 1.340 | 1.403 | | 1.391 | 1.880 | 1.629 | |
| | AVG | 1.020 | 1.390 | 1.390 | | 1.047 | 1.129 | 1.180 | | 1.041 | 1.180 | 1.126 | |
| Golden | MIN | 0.977 | 1.032 | 1.233 | | 1.012 | 0.972 | 0.925 | | 0.951 | 0.968 | 1.086 | |
| | MAX | 1.049 | 1.723 | 2.880 | | 1.095 | 1.234 | 1.288 | | 1.089 | 1.324 | 2.178 | |
| | AVG | 1.014 | 1.364 | 1.683 | | 1.055 | 1.120 | 1.138 | | 1.003 | 1.141 | 1.340 | [2] |
| | | | | | | | | | | | | | |